

Corrigé de l'exercice 1

Développer et réduire chacune des expressions littérales suivantes :

$$\begin{aligned} A &= x \times 6x \\ A &= x \times 6 \times x \\ A &= 6 \times x \times x \\ A &= 6x^2 \end{aligned}$$

$$\begin{aligned} B &= 3x \times 6x \\ B &= 3 \times x \times 6 \times x \\ B &= 3 \times 6 \times x \times x \\ B &= 18x^2 \end{aligned}$$

$$\begin{aligned} C &= 2x + 7 + (9x - 9) \times (6x - 1) \\ C &= 2x + 7 + 9x \times 6x + 9x \times (-1) - 9 \times 6x - 9 \times (-1) \\ C &= 2x + 7 + 9 \times x \times 6 \times x + 9 \times x \times (-1) - 9 \times 6 \times x + 9 \\ C &= 2x + 7 + 9 \times 6 \times x \times x + 9 \times (-1) \times x - 54x + 9 \\ C &= 2x + 7 + 54x^2 - 9x - 54x + 9 \\ C &= 54x^2 + 2x - 9x - 54x + 7 + 9 \\ C &= 54x^2 + (2 - 9 - 54)x + 16 \\ C &= 54x^2 - 61x + 16 \end{aligned}$$

$$\begin{aligned} D &= -10x^2 + (-6x - 5) \times (-4x + 2) \\ D &= -10x^2 - 6x \times (-4x) - 6x \times 2 - 5 \times (-4x) - 5 \times 2 \\ D &= -10x^2 - 6 \times x \times (-4) \times x - 6 \times x \times 2 - 5 \times (-4) \times x - 10 \\ D &= -10x^2 - 6 \times (-4) \times x \times x - 6 \times 2 \times x + 20x - 10 \\ D &= -10x^2 - (-24x^2) - 12x + 20x - 10 \\ D &= 14x^2 - 12x + 20x - 10 \\ D &= 14x^2 + (-12 + 20)x - 10 \\ D &= 14x^2 + 8x - 10 \end{aligned}$$

$$\begin{aligned} E &= 5 + (8x + 1) \times (9x - 4) \\ E &= 5 + 8x \times 9x + 8x \times (-4) + 1 \times 9x + 1 \times (-4) \\ E &= 5 + 8 \times x \times 9 \times x + 8 \times x \times (-4) + 1 \times 9 \times x - 4 \\ E &= 5 + 8 \times 9 \times x \times x + 8 \times (-4) \times x + 9x - 4 \\ E &= 5 + 72x^2 - 32x + 9x - 4 \\ E &= 72x^2 - 32x + 9x + 5 - 4 \\ E &= 72x^2 + (-32 + 9)x + 1 \\ E &= 72x^2 - 23x + 1 \end{aligned}$$

Corrigé de l'exercice 2

Développer et réduire chacune des expressions littérales suivantes :

$$\begin{aligned} A &= x \times 3x \\ A &= x \times 3 \times x \\ A &= 3 \times x \times x \\ A &= 3x^2 \end{aligned}$$

$$\begin{aligned} B &= 9x \times 6x \\ B &= 9 \times x \times 6 \times x \\ B &= 9 \times 6 \times x \times x \\ B &= 54x^2 \end{aligned}$$

$$\begin{aligned} C &= (x + 10) \times (2x - 7) + 7 \\ C &= x \times 2x + x \times (-7) + 10 \times 2x + 10 \times (-7) + 7 \\ C &= x \times 2 \times x - 7 \times x + 10 \times 2 \times x - 70 + 7 \\ C &= 2 \times x \times x - 7x + 20x - 63 \\ C &= 2x^2 - 7x + 20x - 63 \\ C &= 2x^2 + (-7 + 20)x - 63 \end{aligned}$$

$$C = 2x^2 + 13x - 63$$

$$\begin{aligned} D &= -6x - 8 + (5x + 8) \times (7x - 7) \\ D &= -6x - 8 + 5x \times 7x + 5x \times (-7) + 8 \times 7x + 8 \times (-7) \\ D &= -6x - 8 + 5 \times x \times 7 \times x + 5 \times x \times (-7) + 8 \times 7 \times x - 56 \\ D &= -6x - 8 + 5 \times 7 \times x \times x + 5 \times (-7) \times x + 56x - 56 \\ D &= -6x - 8 + 35x^2 - 35x + 56x - 56 \\ D &= 35x^2 - 6x - 35x + 56x - 8 - 56 \\ D &= 35x^2 + (-6 - 35 + 56)x - 64 \\ D &= 35x^2 + 15x - 64 \end{aligned}$$

$$\begin{aligned} E &= -5x^2 + (-8x + 10) \times (5x - 3) \\ E &= -5x^2 - 8x \times 5x - 8x \times (-3) + 10 \times 5x + 10 \times (-3) \\ E &= -5x^2 - 8 \times x \times 5 \times x - 8 \times x \times (-3) + 10 \times 5 \times x - 30 \\ E &= -5x^2 - 8 \times 5 \times x \times x - 8 \times (-3) \times x + 50x - 30 \\ E &= -5x^2 - 40x^2 - (-24x) + 50x - 30 \\ E &= -45x^2 + 24x + 50x - 30 \\ E &= -45x^2 + (24 + 50)x - 30 \\ E &= -45x^2 + 74x - 30 \end{aligned}$$

Corrigé de l'exercice 3

Développer et réduire chacune des expressions littérales suivantes :

$$\begin{aligned} A &= 2x \times x \\ A &= 2 \times x \times x \\ A &= 2x^2 \end{aligned}$$

$$B = 3x \times 4x$$

$$\begin{aligned} B &= 3 \times x \times 4 \times x \\ B &= 3 \times 4 \times x \times x \\ B &= 12x^2 \end{aligned}$$

$$\begin{aligned} C &= (4x + 9) \times (2x - 9) + 3 \\ C &= 4x \times 2x + 4x \times (-9) + 9 \times 2x + 9 \times (-9) + 3 \\ C &= 4 \times x \times 2 \times x + 4 \times x \times (-9) + 9 \times 2 \times x - 81 + 3 \\ C &= 4 \times 2 \times x \times x + 4 \times (-9) \times x + 18x - 78 \\ C &= 8x^2 - 36x + 18x - 78 \\ C &= 8x^2 + (-36 + 18)x - 78 \\ C &= 8x^2 - 18x - 78 \end{aligned}$$

$$\begin{aligned} D &= (10x - 9) \times (-4x + 1) - 6x^2 \\ D &= 10x \times (-4x) + 10x \times 1 - 9 \times (-4x) - 9 \times 1 - 6x^2 \\ D &= 10 \times x \times (-4) \times x + 10 \times x \times 1 - 9 \times (-4) \times x - 9 - 6x^2 \\ D &= 10 \times (-4) \times x \times x + 10 \times x + 36x - 6x^2 - 9 \\ D &= -40x^2 + 10x - 6x^2 + 36x - 9 \\ D &= -40x^2 - 6x^2 + 10x + 36x - 9 \\ D &= (-40 - 6)x^2 + (10 + 36)x - 9 \\ D &= -46x^2 + 46x - 9 \end{aligned}$$

$$\begin{aligned} E &= (-8x - 8) \times (-7x + 7) + 6x - 1 \\ E &= -8x \times (-7x) - 8x \times 7 - 8 \times (-7x) - 8 \times 7 + 6x - 1 \\ E &= -8 \times x \times (-7) \times x - 8 \times x \times 7 - 8 \times (-7) \times x - 56 + 6x - 1 \\ E &= -8 \times (-7) \times x \times x - 8 \times 7 \times x + 56x + 6x - 56 - 1 \end{aligned}$$

$$\begin{aligned} E &= 56x^2 - 56x + (56+6)x - 57 \\ E &= 56x^2 + (-56+56+6)x - 57 \\ \boxed{E = 56x^2 + 6x - 57} \end{aligned}$$

Corrigé de l'exercice 4

Développer et réduire chacune des expressions littérales suivantes :

$$\begin{array}{ll} A = x \times 7x & B = 9x \times 9x \\ A = x \times 7 \times x & B = 9 \times x \times 9 \times x \\ A = 7 \times x \times x & B = 9 \times 9 \times x \times x \\ \boxed{A = 7x^2} & \boxed{B = 81x^2} \end{array}$$

$$\begin{aligned} C &= (-8x+6) \times (7x+4) + x^2 \\ C &= -8x \times 7x - 8x \times 4 + 6 \times 7x + 6 \times 4 + x^2 \\ C &= -8 \times x \times 7 \times x - 8 \times x \times 4 + 6 \times 7 \times x + 24 + x^2 \\ C &= -8 \times 7 \times x \times x - 8 \times 4 \times x + 42x + x^2 + 24 \\ C &= -56x^2 - 32x + x^2 + 42x + 24 \\ C &= -56x^2 + x^2 - 32x + 42x + 24 \\ C &= (-56+1)x^2 + (-32+42)x + 24 \\ \boxed{C = -55x^2 + 10x + 24} \end{aligned}$$

$$\begin{aligned} D &= -8 + (-8x+1) \times (-9x+4) \\ D &= -8 - 8x \times (-9x) - 8x \times 4 + 1 \times (-9x) + 1 \times 4 \\ D &= -8 - 8 \times x \times (-9) \times x - 8 \times x \times 4 + 1 \times (-9) \times x + 4 \\ D &= -8 - 8 \times (-9) \times x \times x - 8 \times 4 \times x - 9x + 4 \\ D &= -8 - (-72x^2) - 32x - 9x + 4 \\ D &= 72x^2 - 32x - 8 - 9x + 4 \\ D &= 72x^2 - 32x - 9x - 8 + 4 \\ D &= 72x^2 + (-32 - 9)x - 4 \\ \boxed{D = 72x^2 - 41x - 4} \end{aligned}$$

$$\begin{aligned} E &= 5x - 7 + (-9x+6) \times (10x+1) \\ E &= 5x - 7 - 9x \times 10x - 9x \times 1 + 6 \times 10x + 6 \times 1 \\ E &= 5x - 7 - 9 \times x \times 10 \times x - 9 \times x \times 1 + 6 \times 10 \times x + 6 \\ E &= 5x - 7 - 9 \times 10 \times x \times x - 9 \times x + 60x + 6 \\ E &= 5x - 7 - 90x^2 - 9x + 60x + 6 \\ E &= -90x^2 + 5x - 9x - 7 + 60x + 6 \\ E &= -90x^2 + 5x - 9x + 60x - 7 + 6 \\ E &= -90x^2 + (5 - 9 + 60)x - 1 \\ \boxed{E = -90x^2 + 56x - 1} \end{aligned}$$

Corrigé de l'exercice 5

Développer et réduire chacune des expressions littérales suivantes :

$$\begin{array}{ll} A = 5x \times x & B = 5x \times 6x \\ A = 5 \times x \times x & B = 5 \times x \times 6 \times x \\ \boxed{A = 5x^2} & \boxed{B = 30x^2} \end{array}$$

$$B = 5 \times 6 \times x \times x$$

$$\boxed{B = 30x^2}$$

$$C = (10x - 6) \times (6x + 3) - 7x - 8$$

$$C = 10x \times 6x + 10x \times 3 - 6 \times 6x - 6 \times 3 - 7x - 8$$

$$C = 10 \times x \times 6 \times x + 10 \times x \times 3 - 6 \times 6 \times x - 18 - 7x - 8$$

$$C = 10 \times 6 \times x \times x + 10 \times 3 \times x - 36x - 7x - 18 - 8$$

$$C = 60x^2 + 30x(-36 - 7)x - 26$$

$$C = 60x^2 + (30 + (-36) - 7)x - 26$$

$$\boxed{C = 60x^2 - 13x - 26}$$

$$D = 10x^2 + (10x - 7) \times (6x + 6)$$

$$D = 10x^2 + 10x \times 6x + 10x \times 6 - 7 \times 6x - 7 \times 6$$

$$D = 10x^2 + 10 \times x \times 6 \times x + 10 \times x \times 6 - 7 \times 6 \times x - 42$$

$$D = 10x^2 + 10 \times 6 \times x \times x + 10 \times 6 \times x - 42x - 42$$

$$D = 10x^2 + 60x^2 + 60x - 42x - 42$$

$$D = (10 + 60)x^2 + (60 - 42)x - 42$$

$$\boxed{D = 70x^2 + 18x - 42}$$

$$E = -5 + (-6x + 3) \times (-5x + 4)$$

$$E = -5 - 6x \times (-5x) - 6x \times 4 + 3 \times (-5x) + 3 \times 4$$

$$E = -5 - 6 \times x \times (-5) \times x - 6 \times x \times 4 + 3 \times (-5) \times x + 12$$

$$E = -5 - 6 \times (-5) \times x \times x - 6 \times 4 \times x - 15x + 12$$

$$E = -5 - (-30x^2) - 24x - 15x + 12$$

$$E = 30x^2 - 24x - 5 - 15x + 12$$

$$E = 30x^2 - 24x - 15x - 5 + 12$$

$$E = 30x^2 + (-24 - 15)x + 7$$

$$\boxed{E = 30x^2 - 39x + 7}$$

Corrigé de l'exercice 6

Développer et réduire chacune des expressions littérales suivantes :

$$A = x \times 8x$$

$$A = x \times 8 \times x$$

$$A = 8 \times x \times x$$

$$\boxed{A = 8x^2}$$

$$B = 9x \times 7x$$

$$B = 9 \times x \times 7 \times x$$

$$B = 9 \times 7 \times x \times x$$

$$\boxed{B = 63x^2}$$

$$C = (-5x + 4) \times (7x + 2) + x^2$$

$$C = -5x \times 7x - 5x \times 2 + 4 \times 7x + 4 \times 2 + x^2$$

$$C = -5 \times x \times 7 \times x - 5 \times x \times 2 + 4 \times 7 \times x + 8 + x^2$$

$$C = -5 \times 7 \times x \times x - 5 \times 2 \times x + 28x + x^2 + 8$$

$$C = -35x^2 - 10x + x^2 + 28x + 8$$

$$C = -35x^2 + x^2 - 10x + 28x + 8$$

$$C = (-35 + 1)x^2 + (-10 + 28)x + 8$$

$$\boxed{C = -34x^2 + 18x + 8}$$

$$D = 4x + 9 + (4x - 4) \times (-4x + 3)$$

$$D = 4x + 9 + 4x \times (-4x) + 4x \times 3 - 4 \times (-4x) - 4 \times 3$$

$$D = 4x + 9 + 4 \times x \times (-4) \times x + 4 \times x \times 3 - 4 \times (-4) \times x - 12$$

$$D = 4x + 9 + 4 \times (-4) \times x \times x + 4 \times 3 \times x + 16x - 12$$

$$D = 4x + 9 - 16x^2 + 12x + 16x - 12$$

$$D = -16x^2 + 4x + 12x + 16x + 9 - 12$$

$$D = -16x^2 + (4 + 12 + 16)x - 3$$

$$D = -16x^2 + 32x - 3$$

$$E = 6 + (-7x - 6) \times (5x - 3)$$

$$E = 6 - 7x \times 5x - 7x \times (-3) - 6 \times 5x - 6 \times (-3)$$

$$E = 6 - 7 \times x \times 5 \times x - 7 \times x \times (-3) - 6 \times 5 \times x + 18$$

$$E = 6 - 7 \times 5 \times x \times x - 7 \times (-3) \times x - 30x + 18$$

$$E = 6 - 35x^2 - (-21x) - 30x + 18$$

$$E = -35x^2 + 21x + 6 - 30x + 18$$

$$E = -35x^2 + 21x - 30x + 6 + 18$$

$$E = -35x^2 + (21 - 30)x + 24$$

$$E = -35x^2 - 9x + 24$$