

Corrigé de l'exercice 1

Développer et réduire chacune des expressions littérales suivantes :

$$A = 4x \times x$$

$$A = 4 \times x \times x$$

$A = 4x^2$

$$B = 4x \times 4x$$

$$B = 4 \times x \times 4 \times x$$

$$B = 4 \times 4 \times x \times x$$

$B = 16x^2$

$$\begin{aligned} C &= -3x^2 + (-6x - 7) \times (-5x - 9) \\ &= -3x^2 - 6x \times (-5x) - 6x \times (-9) - 7 \times (-5x) - 7 \times (-9) \\ &= -3x^2 - 6 \times x \times (-5) \times x - 6 \times x \times (-9) - 7 \times (-5) \times x + 63 \\ &= -3x^2 - 6 \times (-5) \times x \times x - 6 \times (-9) \times x + 35x + 63 \\ &= -3x^2 - (-30x^2) - (-54x) + 35x + 63 \\ &= 27x^2 + 54x + 35x + 63 \\ &= 27x^2 + (54 + 35)x + 63 \\ &\boxed{C = 27x^2 + 89x + 63} \end{aligned}$$

$$D = 2 + (4x + 10) \times (6x - 6)$$

$$\begin{aligned} D &= 2 + 4x \times 6x + 4x \times (-6) + 10 \times 6x + 10 \times (-6) \\ &= 2 + 4 \times x \times 6 \times x + 4 \times x \times (-6) + 10 \times 6 \times x - 60 \\ &= 2 + 4 \times 6 \times x \times x + 4 \times (-6) \times x + 60x - 60 \\ &= 2 + 24x^2 - 24x + 60x - 60 \\ &= 24x^2 - 24x + 60x + 2 - 60 \\ &= 24x^2 + (-24 + 60)x - 58 \\ &\boxed{D = 24x^2 + 36x - 58} \end{aligned}$$

$$E = (10x + 9) \times (-4x + 10) + 8x - 10$$

$$\begin{aligned} E &= 10x \times (-4x) + 10x \times 10 + 9 \times (-4x) + 9 \times 10 + 8x - 10 \\ &= 10 \times x \times (-4) \times x + 10 \times x \times 10 + 9 \times (-4) \times x + 90 + 8x - 10 \\ &= 10 \times (-4) \times x \times x + 10 \times 10 \times x - 36x + 8x + 90 - 10 \\ &= -40x^2 + 100x(-36 + 8)x + 80 \\ &= -40x^2 + (100 + (-36) + 8)x + 80 \\ &\boxed{E = -40x^2 + 72x + 80} \end{aligned}$$

Corrigé de l'exercice 2

Développer et réduire chacune des expressions littérales suivantes :

$$A = 7x \times x$$

$$A = 7 \times x \times x$$

$A = 7x^2$

$$B = 2x \times 9x$$

$$B = 2 \times x \times 9 \times x$$

$$B = 2 \times 9 \times x \times x$$

$B = 18x^2$

$$\begin{aligned} C &= x - 10 + (8x + 6) \times (7x - 5) \\ &= x - 10 + 8x \times 7x + 8x \times (-5) + 6 \times 7x + 6 \times (-5) \\ &= x - 10 + 8 \times x \times 7 \times x + 8 \times x \times (-5) + 6 \times 7 \times x - 30 \\ &= x - 10 + 8 \times 7 \times x \times x + 8 \times (-5) \times x + 42x - 30 \\ &= x - 10 + 56x^2 - 40x + 42x - 10 - 30 \\ &= 56x^2 + x - 40x + 42x - 10 - 30 \\ &= 56x^2 + (1 - 40 + 42)x - 40 \end{aligned}$$

$$C = 56x^2 + 3x - 40$$

$$D = 10 + (-7x + 4) \times (-9x - 6)$$

$$D = 10 - 7x \times (-9x) - 7x \times (-6) + 4 \times (-9x) + 4 \times (-6)$$

$$D = 10 - 7 \times x \times (-9) \times x - 7 \times x \times (-6) + 4 \times (-9) \times x - 24$$

$$D = 10 - 7 \times (-9) \times x \times x - 7 \times (-6) \times x - 36x - 24$$

$$D = 10 - (-63x^2) - (-42x) - 36x - 24$$

$$D = 63x^2 + 42x + 10 - 36x - 24$$

$$D = 63x^2 + 42x - 36x + 10 - 24$$

$$D = 63x^2 + (42 - 36)x - 14$$

$$D = 63x^2 + 6x - 14$$

$$E = (-9x - 6) \times (6x + 9) + 2x^2$$

$$E = -9x \times 6x - 9x \times 9 - 6 \times 6x - 6 \times 9 + 2x^2$$

$$E = -9 \times x \times 6 \times x - 9 \times x \times 9 - 6 \times 6 \times x - 54 + 2x^2$$

$$E = -9 \times 6 \times x \times x - 9 \times 9 \times x - 36x + 2x^2 - 54$$

$$E = -54x^2 - 81x + 2x^2 - 36x - 54$$

$$E = -54x^2 + 2x^2 - 81x - 36x - 54$$

$$E = (-54 + 2)x^2 + (-81 - 36)x - 54$$

$$E = -52x^2 - 117x - 54$$

Corrigé de l'exercice 3

Développer et réduire chacune des expressions littérales suivantes :

$$A = x \times 7x$$

$$A = x \times 7 \times x$$

$$A = 7 \times x \times x$$

$$A = 7x^2$$

$$B = 9x \times 3x$$

$$B = 9 \times x \times 3 \times x$$

$$B = 9 \times 3 \times x \times x$$

$$B = 27x^2$$

$$C = (-5x + 10) \times (-x + 8) - 7x + 3$$

$$C = -5x \times (-x) - 5x \times 8 + 10 \times (-x) + 10 \times 8 - 7x + 3$$

$$C = -5 \times x \times (-1) \times x - 5 \times x \times 8 + 10 \times (-1) \times x + 80 - 7x + 3$$

$$C = -5 \times (-1) \times x \times x - 5 \times 8 \times x - 10x - 7x + 80 + 3$$

$$C = 5x^2 - 40x(-10 - 7)x + 83$$

$$C = 5x^2 + (-40 + (-10) - 7)x + 83$$

$$C = 5x^2 - 57x + 83$$

$$D = (2x - 10) \times (-4x - 6) - 9$$

$$D = 2x \times (-4x) + 2x \times (-6) - 10 \times (-4x) - 10 \times (-6) - 9$$

$$D = 2 \times x \times (-4) \times x + 2 \times x \times (-6) - 10 \times (-4) \times x + 60 - 9$$

$$D = 2 \times (-4) \times x \times x + 2 \times (-6) \times x + 40x + 51$$

$$D = -8x^2 - 12x + 40x + 51$$

$$D = -8x^2 + (-12 + 40)x + 51$$

$$D = -8x^2 + 28x + 51$$

$$E = (-2x - 4) \times (3x + 2) + 4x^2$$

$$E = -2x \times 3x - 2x \times 2 - 4 \times 3x - 4 \times 2 + 4x^2$$

$$E = -2 \times x \times 3 \times x - 2 \times x \times 2 - 4 \times 3 \times x - 8 + 4x^2$$

$$E = -2 \times 3 \times x \times x - 2 \times 2 \times x - 12x + 4x^2 - 8$$

$$\begin{aligned} E &= -6x^2 - 4x + 4x^2 - 12x - 8 \\ E &= -6x^2 + 4x^2 - 4x - 12x - 8 \\ E &= (-6+4)x^2 + (-4-12)x - 8 \\ E &= -2x^2 - 16x - 8 \end{aligned}$$

Corrigé de l'exercice 4

Développer et réduire chacune des expressions littérales suivantes :

$$\begin{array}{ll} A = 7x \times x & B = 3 \times x \times 5 \times x \\ A = 7 \times x \times x & B = 3 \times 5 \times x \times x \\ A = 7x^2 & B = 15x^2 \end{array}$$

$$B = 3x \times 5x$$

$$\begin{aligned} C &= 3x^2 + (3x-5) \times (-7x-10) \\ C &= 3x^2 + 3x \times (-7x) + 3x \times (-10) - 5 \times (-7x) - 5 \times (-10) \\ C &= 3x^2 + 3 \times x \times (-7) \times x + 3 \times x \times (-10) - 5 \times (-7) \times x + 50 \\ C &= 3x^2 + 3 \times (-7) \times x \times x + 3 \times (-10) \times x + 35x + 50 \\ C &= 3x^2 - 21x^2 - 30x + 35x + 50 \\ C &= (3-21)x^2 + (-30+35)x + 50 \\ C &= -18x^2 + 5x + 50 \end{aligned}$$

$$\begin{aligned} D &= 3 + (3x+2) \times (7x-6) \\ D &= 3 + 3x \times 7x + 3x \times (-6) + 2 \times 7x + 2 \times (-6) \\ D &= 3 + 3 \times x \times 7 \times x + 3 \times x \times (-6) + 2 \times 7 \times x - 12 \\ D &= 3 + 3 \times 7 \times x \times x + 3 \times (-6) \times x + 14x - 12 \\ D &= 3 + 21x^2 - 18x + 14x - 12 \\ D &= 21x^2 - 18x + 14x + 3 - 12 \\ D &= 21x^2 + (-18+14)x - 9 \\ D &= 21x^2 - 4x - 9 \end{aligned}$$

$$\begin{aligned} E &= (-5x-3) \times (-7x+6) + 2x + 7 \\ E &= -5x \times (-7x) - 5x \times 6 - 3 \times (-7x) - 3 \times 6 + 2x + 7 \\ E &= -5 \times x \times (-7) \times x - 5 \times x \times 6 - 3 \times (-7) \times x - 18 + 2x + 7 \\ E &= -5 \times (-7) \times x \times x - 5 \times 6 \times x + 21x + 2x - 18 + 7 \\ E &= 35x^2 - 30x + (21+2)x - 11 \\ E &= 35x^2 + (-30+21+2)x - 11 \\ E &= 35x^2 - 7x - 11 \end{aligned}$$

Corrigé de l'exercice 5

Développer et réduire chacune des expressions littérales suivantes :

$$\begin{array}{ll} A = x \times 4x & B = 4x \times 9x \\ A = x \times 4 \times x & B = 4 \times x \times 9 \times x \\ A = 4 \times x \times x & B = 4 \times 9 \times x \times x \\ A = 4x^2 & B = 36x^2 \end{array}$$

$$\begin{aligned} C &= 3x^2 + (3x-3) \times (-8x+2) \\ C &= 3x^2 + 3x \times (-8x) + 3x \times 2 - 3 \times (-8x) - 3 \times 2 \end{aligned}$$

$$\begin{aligned}
 C &= 3x^2 + 3 \times x \times (-8) \times x + 3 \times x \times 2 - 3 \times (-8) \times x - 6 \\
 C &= 3x^2 + 3 \times (-8) \times x \times x + 3 \times 2 \times x + 24x - 6 \\
 C &= 3x^2 - 24x^2 + 6x + 24x - 6 \\
 C &= (3 - 24)x^2 + (6 + 24)x - 6 \\
 C &= -21x^2 + 30x - 6
 \end{aligned}$$

$$\begin{aligned}
 D &= -7 + (-2x + 6) \times (2x - 7) \\
 D &= -7 - 2x \times 2x - 2x \times (-7) + 6 \times 2x + 6 \times (-7) \\
 D &= -7 - 2 \times x \times 2 \times x - 2 \times x \times (-7) + 6 \times 2 \times x - 42 \\
 D &= -7 - 2 \times 2 \times x \times x - 2 \times (-7) \times x + 12x - 42 \\
 D &= -7 - 4x^2 - (-14x) + 12x - 42 \\
 D &= -4x^2 + 14x - 7 + 12x - 42 \\
 D &= -4x^2 + 14x + 12x - 7 - 42 \\
 D &= -4x^2 + (14 + 12)x - 49 \\
 D &= -4x^2 + 26x - 49
 \end{aligned}$$

$$\begin{aligned}
 E &= (3x - 4) \times (-2x + 1) - 9x + 4 \\
 E &= 3x \times (-2x) + 3x \times 1 - 4 \times (-2x) - 4 \times 1 - 9x + 4 \\
 E &= 3 \times x \times (-2) \times x + 3 \times x \times 1 - 4 \times (-2) \times x - 4 - 9x + 4 \\
 E &= 3 \times (-2) \times x \times x + 3 \times x + 8x - 9x - 4 + 4 \\
 E &= -6x^2 + 3x(8 - 9)x \\
 E &= -6x^2 + (3 + 8 - 9)x \\
 E &= -6x^2 + 2x
 \end{aligned}$$

Corrigé de l'exercice 6

Développer et réduire chacune des expressions littérales suivantes :

$ \begin{aligned} A &= 7x \times x \\ A &= 7 \times x \times x \\ A &= 7x^2 \end{aligned} $	$ \begin{aligned} B &= 4 \times x \times 9 \times x \\ B &= 4 \times 9 \times x \times x \\ B &= 36x^2 \end{aligned} $
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$$B = 4x \times 9x$$

$$\begin{aligned}
 C &= 9x^2 + (-9x + 6) \times (9x + 1) \\
 C &= 9x^2 - 9x \times 9x - 9x \times 1 + 6 \times 9x + 6 \times 1 \\
 C &= 9x^2 - 9 \times x \times 9 \times x - 9 \times x \times 1 + 6 \times 9 \times x + 6 \\
 C &= 9x^2 - 9 \times 9 \times x \times x - 9 \times x + 54x + 6 \\
 C &= 9x^2 - 81x^2 - 9x + 54x + 6 \\
 C &= -72x^2 - 9x + 54x + 6 \\
 C &= -72x^2 + (-9 + 54)x + 6 \\
 C &= -72x^2 + 45x + 6
 \end{aligned}$$

$$\begin{aligned}
 D &= (-10x + 5) \times (9x - 2) - 3x + 2 \\
 D &= -10x \times 9x - 10x \times (-2) + 5 \times 9x + 5 \times (-2) - 3x + 2 \\
 D &= -10 \times x \times 9 \times x - 10 \times x \times (-2) + 5 \times 9 \times x - 10 - 3x + 2 \\
 D &= -10 \times 9 \times x \times x - 10 \times (-2) \times x + 45x - 3x - 10 + 2 \\
 D &= -90x^2 - (-20x) + (45 - 3)x - 8 \\
 D &= -90x^2 + 20x + (45 - 3)x - 8 \\
 D &= -90x^2 + (20 + 45 - 3)x - 8 \\
 D &= -90x^2 + 62x - 8
 \end{aligned}$$

$$\begin{aligned}E &= (-10x - 9) \times (8x - 2) + 2 \\E &= -10x \times 8x - 10x \times (-2) - 9 \times 8x - 9 \times (-2) + 2 \\E &= -10 \times x \times 8 \times x - 10 \times x \times (-2) - 9 \times 8 \times x + 18 + 2 \\E &= -10 \times 8 \times x \times x - 10 \times (-2) \times x - 72x + 20 \\E &= -80x^2 - (-20x) - 72x + 20 \\E &= -80x^2 + 20x - 72x + 20 \\E &= -80x^2 + (20 - 72)x + 20 \\E &= -80x^2 - 52x + 20\end{aligned}$$