

Corrigé de l'exercice 1

Factoriser chacune des expressions littérales suivantes :

$$A = 9x^2 - 42x + 49$$

$$A = (3x)^2 - 2 \times 3x \times 7 + 7^2$$

$$A = (3x - 7)^2$$

$$B = (6x + 5) \times (-7x + 2) + (5x - 5) \times (6x + 5)$$

$$B = (6x + 5) \times (-7x + 2 + 5x - 5)$$

$$B = (6x + 5) \times (-7x + 5x + 2 - 5)$$

$$B = (6x + 5) \times (-2x - 3)$$

$$C = 100x^2 - 100$$

$$C = (\sqrt{100}x)^2 - \sqrt{100}^2$$

$$C = (\sqrt{100}x + \sqrt{100}) \times (\sqrt{100}x - \sqrt{100})$$

$$C = (10x + 10) \times (10x - 10)$$

$$D = (x - 7)^2 - 16$$

$$D = (x - 7)^2 - 4^2$$

$$D = (x - 7 + 4) \times (x - 7 - 4)$$

$$D = (x - 3) \times (x - 11)$$

$$E = (10x + 2) \times (10x + 8) - (10x + 2)$$

$$E = (10x + 2) \times (10x + 8) - (10x + 2) \times 1$$

$$E = (10x + 2) \times (10x + 8 - 1)$$

$$E = (10x + 2) \times (10x + 7)$$

$$F = (2x - 5) \times (8x + 10) + (8x + 10)^2$$

$$F = (2x - 5) \times (8x + 10) + (8x + 10) \times (8x + 10)$$

$$F = (8x + 10) \times (2x - 5 + 8x + 10)$$

$$F = (8x + 10) \times (2x + 8x - 5 + 10)$$

$$F = (8x + 10) \times (10x + 5)$$

Corrigé de l'exercice 2

Factoriser chacune des expressions littérales suivantes :

$$A = x^2 - 8x + 16$$

$$A = x^2 - 2 \times x \times 4 + 4^2$$

$$A = (x - 4)^2$$

$$B = -(x + 9)^2 + 16$$

$$B = -(x + 9)^2 + 4^2$$

$$B = (4 + x + 9) \times (4 - (x + 9))$$

$$B = (x + 4 + 9) \times (4 - x - 9)$$

$$B = (x + 4 + 9) \times (-x + 4 - 9)$$

$$B = (x + 13) \times (-x - 5)$$

$$C = (x + 5) \times (3x + 10) + (x + 5) \times (4x + 10)$$

$$C = (x + 5) \times (3x + 10 + 4x + 10)$$

$$C = (x + 5) \times (3x + 4x + 10 + 10)$$

$$C = (x + 5) \times (7x + 20)$$

$$D = 81x^2 - 36$$

$$D = (\sqrt{81}x)^2 - \sqrt{36}^2$$

$$D = (\sqrt{81}x + \sqrt{36}) \times (\sqrt{81}x - \sqrt{36})$$

$$D = (9x + 6) \times (9x - 6)$$

$$E = (3x - 4)^2 + (3x - 4) \times (6x + 9)$$

$$E = (3x - 4) \times (3x - 4) + (3x - 4) \times (6x + 9)$$

$$E = (3x - 4) \times (3x - 4 + 6x + 9)$$

$$E = (3x - 4) \times (3x + 6x - 4 + 9)$$

$$E = (3x - 4) \times (9x + 5)$$

$$F = -(7x + 5) \times (4x + 1) + 7x + 5$$

$$F = -(7x + 5) \times (4x + 1) + (7x + 5) \times 1$$

$$F = (7x + 5) \times (-(4x + 1) + 1)$$

$$F = (7x + 5) \times (-4x - 1 + 1)$$

$$F = (7x + 5) \times (-4x)$$

Corrigé de l'exercice 3

Factoriser chacune des expressions littérales suivantes :

$$A = (-5x - 7) \times (10x - 10) + (-5x - 7) \times (-8x + 6)$$

$$A = (-5x - 7) \times (10x - 10 - 8x + 6)$$

$$A = (-5x - 7) \times (10x - 8x - 10 + 6)$$

$$A = (-5x - 7) \times (2x - 4)$$

$$B = x^2 + 16x + 64$$

$$B = x^2 + 2 \times x \times 8 + 8^2$$

$$B = (x + 8)^2$$

$$\begin{aligned} C &= (x+8)^2 - 49x^2 \\ C &= (x+8)^2 - (7x)^2 \\ C &= (x+8+7x) \times (x+8-7x) \\ C &= (x+7x+8) \times (x-7x+8) \\ C &= (8x+8) \times (-6x+8) \end{aligned}$$

$$\begin{aligned} D &= 4x^2 - 16 \\ D &= (\sqrt{4}x)^2 - \sqrt{16}^2 \\ D &= (\sqrt{4}x + \sqrt{16}) \times (\sqrt{4}x - \sqrt{16}) \\ D &= (2x+4) \times (2x-4) \end{aligned}$$

$$E = -(6x-3) + (2x-3) \times (6x-3)$$

$$\begin{aligned} E &= -(6x-3) \times 1 + (2x-3) \times (6x-3) \\ E &= (6x-3) \times (-1+2x-3) \\ E &= (6x-3) \times (2x-1-3) \\ E &= (6x-3) \times (2x-4) \end{aligned}$$

$$\begin{aligned} F &= (-9x+10) \times (7x-1) + (-9x+10)^2 \\ F &= (-9x+10) \times (7x-1) + (-9x+10) \times (-9x+10) \\ F &= (-9x+10) \times (7x-1-9x+10) \\ F &= (-9x+10) \times (7x-9x-1+10) \\ F &= (-9x+10) \times (-2x+9) \end{aligned}$$

Corrigé de l'exercice 4

Factoriser chacune des expressions littérales suivantes :

$$\begin{aligned} A &= (9x+8) \times (x-2) + (5x+1) \times (9x+8) \\ A &= (9x+8) \times (x-2+5x+1) \\ A &= (9x+8) \times (x+5x-2+1) \\ A &= (9x+8) \times (6x-1) \end{aligned}$$

$$\begin{aligned} B &= 100x^2 - 140x + 49 \\ B &= (10x)^2 - 2 \times 10x \times 7 + 7^2 \\ B &= (10x-7)^2 \end{aligned}$$

$$\begin{aligned} C &= (-x+8)^2 - 64 \\ C &= (-x+8)^2 - 8^2 \\ C &= (-x+8+8) \times (-x+8-8) \\ C &= (-x+16) \times (-x) \end{aligned}$$

$$\begin{aligned} D &= -25x^2 + 25 \\ D &= \sqrt{25}^2 - (\sqrt{25}x)^2 \\ D &= (\sqrt{25} + \sqrt{25}x) \times (\sqrt{25} - \sqrt{25}x) \end{aligned}$$

$$\begin{aligned} D &= (\sqrt{25}x + \sqrt{25}) \times (5 - 5x) \\ D &= (\sqrt{25}x + \sqrt{25}) \times (-5x + 5) \\ D &= (5x + 5) \times (-5x + 5) \end{aligned}$$

$$\begin{aligned} E &= -(7x-1) \times (x+5) + x+5 \\ E &= -(7x-1) \times (x+5) + (x+5) \times 1 \\ E &= (x+5) \times (-7x+1+1) \\ E &= (x+5) \times (-7x+1+1) \\ E &= (x+5) \times (-7x+2) \end{aligned}$$

$$\begin{aligned} F &= (9x+2) \times (10x+8) + (9x+2)^2 \\ F &= (9x+2) \times (10x+8) + (9x+2) \times (9x+2) \\ F &= (9x+2) \times (10x+8+9x+2) \\ F &= (9x+2) \times (10x+9x+8+2) \\ F &= (9x+2) \times (19x+10) \end{aligned}$$

Corrigé de l'exercice 5

Factoriser chacune des expressions littérales suivantes :

$$\begin{aligned} A &= (5x+3) \times (3x+10) + (-x+8) \times (5x+3) \\ A &= (5x+3) \times (3x+10-x+8) \\ A &= (5x+3) \times (3x-x+10+8) \\ A &= (5x+3) \times (2x+18) \end{aligned}$$

$$\begin{aligned} B &= (6x-8)^2 - 64x^2 \\ B &= (6x-8)^2 - (8x)^2 \\ B &= (6x-8+8x) \times (6x-8-8x) \\ B &= (6x+8x-8) \times (6x-8x-8) \\ B &= (14x-8) \times (-2x-8) \end{aligned}$$

$$\begin{aligned} C &= 4x^2 - 8x + 4 \\ C &= (2x)^2 - 2 \times 2x \times 2 + 2^2 \\ C &= (2x-2)^2 \end{aligned}$$

$$\begin{aligned} D &= 49x^2 - 100 \\ D &= (\sqrt{49}x)^2 - \sqrt{100}^2 \\ D &= (\sqrt{49}x + \sqrt{100}) \times (\sqrt{49}x - \sqrt{100}) \\ D &= (7x+10) \times (7x-10) \end{aligned}$$

$$E = 4x+1 + (4x+1) \times (5x+3)$$

$$\begin{aligned} E &= (4x + 1) \times 1 + (4x + 1) \times (5x + 3) \\ E &= (4x + 1) \times (1 + 5x + 3) \\ E &= (4x + 1) \times (5x + 1 + 3) \\ \boxed{E = (4x + 1) \times (5x + 4)} \end{aligned}$$

$$F = (x + 4) \times (8x + 2) - (8x + 2)^2$$

$$\begin{aligned} F &= (x + 4) \times (8x + 2) - (8x + 2) \times (8x + 2) \\ F &= (8x + 2) \times (x + 4 - (8x + 2)) \\ F &= (8x + 2) \times (x + 4 - 8x - 2) \\ F &= (8x + 2) \times (x - 8x + 4 - 2) \\ \boxed{F = (8x + 2) \times (-7x + 2)} \end{aligned}$$

Corrigé de l'exercice 6

Factoriser chacune des expressions littérales suivantes :

$$\begin{aligned} A &= (5x + 10) \times (x + 4) + (-7x - 9) \times (x + 4) \\ A &= (x + 4) \times (5x + 10 - 7x - 9) \\ A &= (x + 4) \times (5x - 7x + 10 - 9) \\ \boxed{A = (x + 4) \times (-2x + 1)} \end{aligned}$$

$$\begin{aligned} B &= 49x^2 + 126x + 81 \\ B &= (7x)^2 + 2 \times 7x \times 9 + 9^2 \\ \boxed{B = (7x + 9)^2} \end{aligned}$$

$$\begin{aligned} C &= x^2 - (5x - 8)^2 \\ C &= (x + 5x - 8) \times (x - (5x - 8)) \\ C &= (6x - 8) \times (x - 5x + 8) \\ \boxed{C = (6x - 8) \times (-4x + 8)} \end{aligned}$$

$$\begin{aligned} D &= -64x^2 + 9 \\ D &= \sqrt{9}^2 - (\sqrt{64}x)^2 \\ D &= (\sqrt{9} + \sqrt{64}x) \times (\sqrt{9} - \sqrt{64}x) \end{aligned}$$

$$\begin{aligned} D &= (\sqrt{64}x + \sqrt{9}) \times (3 - 8x) \\ D &= (\sqrt{64}x + \sqrt{9}) \times (-8x + 3) \\ \boxed{D = (8x + 3) \times (-8x + 3)} \end{aligned}$$

$$\begin{aligned} E &= (6x + 10) \times (4x + 6) - (6x + 10)^2 \\ E &= (6x + 10) \times (4x + 6) - (6x + 10) \times (6x + 10) \\ E &= (6x + 10) \times (4x + 6 - (6x + 10)) \\ E &= (6x + 10) \times (4x + 6 - 6x - 10) \\ E &= (6x + 10) \times (4x - 6x + 6 - 10) \\ \boxed{E = (6x + 10) \times (-2x - 4)} \end{aligned}$$

$$\begin{aligned} F &= (9x + 10) \times (9x + 2) + 9x + 2 \\ F &= (9x + 10) \times (9x + 2) + (9x + 2) \times 1 \\ F &= (9x + 2) \times (9x + 10 + 1) \\ \boxed{F = (9x + 2) \times (9x + 11)} \end{aligned}$$